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What is claimed is:

1. A method of substrate modeling, comprising:
determining scalable Z parameters associated with at least two substrate
5 contacts;
constructing a matrix of the scalable Z parameters for the at least two substrate
contacts; and
calculating an inverse of the matrix to determine resistance values associated
with the at least two substrate contacts.
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2. The method of claim 1, wherein the number of contacts is N , and the
matrix is an $N \times N$ matrix.
3. The method of claim 1, wherein the substrate is a heavily doped
15 substrate.
4. The method of claim 1, wherein the substrate is a lightly doped substrate.
5. The method of claim 1, wherein, for a first contact and a second contact
20 of the at least two contacts, the determining comprises:
dividing the first contact into smaller portions; and
determining respective Z parameters between the smaller portions and the
second contact.
- 25 6. The method of claim 5, wherein the smaller portions are rectangular or
square portions.

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7. The method of claim 1, wherein, for a first contact and a second contact of the at least two contacts, three scalable Z parameters are determined.

8. The method of claim 7, wherein a first of the scalable Z parameters is a ratio of an open-circuit voltage at the first contact to an input current at the first contact, a second of the scalable Z parameters is a ratio of an open-circuit voltage at the second contact to an input current at the second contact, and a third of the scalable Z parameters is a ratio of an open-circuit voltage at the first contact to a source current at the second contact.

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9. The method of claim 1, wherein at least one of the scalable Z parameters is a function of contact area and contact perimeter.

10. The method of claim 1, wherein at least one of the scalable Z parameters is a function of contact geometry and contact separation.

11. The method of claim 1, wherein the scalable Z parameters comprise a first set of scalable Z parameters associated with resistances between the at least two substrate contacts and a groundplane and a second set of scalable Z parameters associated with cross-coupling resistances between the at least two substrate contacts.

12. The method of claim 11, wherein the scalable Z parameters of the first set are based on a first model equation and the scalable Z parameters of the second set are based on a second model equation.

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13. The method of claim 12, wherein the first model equation is

$$Z = \frac{1}{K_1 Area + K_2 Perimeter + K_3},$$

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wherein Z is a ratio of an open-circuit voltage to input current for a selected contact with other contacts being open circuits, $Area$ is an area of the selected contact, $Perimeter$ is a perimeter of the selected contact, and K_1 , K_2 , and K_3 are parameters that are dependent on substrate properties.

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14. The method of claim 13, wherein K_1 , K_2 , and K_3 are determined by curve fitting based on a simulation or a measurement.

15. The method of claim 12, wherein the substrate is a lightly doped
10 substrate, and the first model equation is

$$Z = \frac{1}{K_1 Perimeter + K_2},$$

wherein Z is a ratio of an open-circuit voltage to an input current for a selected contact with other contacts being open circuits, $Perimeter$ is a perimeter of the selected contact, and K_1 and K_2 are parameters that are dependent on substrate properties.

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16. The method of claim 15, wherein K_1 and K_2 are determined by curve fitting based on a simulation or a measurement.

17. The method of claim 12, wherein the second model equation for a
20 selected pair of contacts having a fixed relative position y is

$$Z = \alpha e^{-\beta x},$$

wherein Z is a ratio of an open-circuit voltage at a first contact to a source current at a second contact, x is a separation between the first contact and the second contact, α is a value of Z when x is zero, and β is a parameter that is dependent on substrate properties.

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18. The method of claim 17, wherein the first contact and the second contact of the selected pair of contacts have a same contact size.

19. The method of claim 17, wherein β is determined by curve fitting based
5 on a simulation or a measurement.

20. The method of claim 12, wherein the second model equation for a selected pair of contacts having a fixed separation x is

$$Z = ay^2 + by + c,$$

10 wherein Z is a ratio of an open-circuit voltage at a first contact to a source current at a second contact, y is a relative position between the first contact and the second contact, and a , b , and c are scalable parameters that substantially depend on contact dimensions.

21. The method of claim 20, wherein a size of the first contact is different
15 than a size of the second contact.

22. The method of claim 20, wherein at least one of the parameters a , b , or c is determined by curve fitting based on a simulation or a measurement.

20 23. The method of claim 12, wherein the second model equation for a selected pair of contacts is

$$Z = [ay^2 + by + c]e^{-\beta(x-x_a)},$$

wherein Z is a ratio of an open-circuit voltage at a first contact to a source current at a second contact, y is a relative position between the first contact and the second contact,
25 a , b , and c are scalable parameters for the substrate that depend on contact dimensions, x is a separation between the first contact and the second contact, x_a is a value of x used

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in determining a , b , and c , and β is a parameter that is dependent on substrate properties.

24. The method of claim 23, wherein a size of the first contact is different
5 than a size of the second contact.

25. The method of claim 23, wherein at least one of the parameters a , b , c or β is determined by curve fitting based on a simulation or a measurement.

10 26. The method of claim 12, wherein the substrate is a lightly doped substrate, and the second model equation for a selected pair of contacts having a fixed relative position y is

$$Z = \alpha K_0(\beta x),$$

wherein Z is a ratio of an open-circuit voltage at a first contact to a source current at a
15 second contact, K_0 is a 0th-order Bessel function of the second kind, x is a separation between the first contact and the second contact, and α and β are parameters that are dependent on substrate properties.

27. The method of claim 12, wherein the substrate is a lightly doped
20 substrate and the second model equation for a selected pair of contacts predicts a value Z as a function of a separation x between the first contact and the second contact, wherein Z is a ratio of an open-circuit voltage at a first contact to a source current at a second contact, and $\log(Z)$ has a linear behavior when x is greater than a certain value and an asymptotic-like behavior when x is less than the certain value.

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28. A computer-readable medium storing computer-executable instructions for causing a computer system to perform the method of claim 1.

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29. A method of substrate modeling, comprising:
determining scalable parameters associated with at least two substrate contacts,
at least one of the scalable parameters being scalable with a contact perimeter;
5 constructing a matrix of the scalable parameters for the at least two substrate
contacts; and
calculating an inverse of the matrix to determine resistance values associated
with the at least two substrate contacts.
- 10 30. The method of claim 29, wherein the scalable parameters are Z
parameters.
31. The method of claim 29, wherein at least one of the scalable parameters
is scalable with a contact separation.
- 15 32. The method of claim 29, wherein the scalable parameters comprise a first
set of scalable parameters associated with resistances between the at least two substrate
contacts and a groundplane and a second set of scalable parameters associated with
cross-coupling resistances between the at least two substrate contacts.
- 20 33. The method of claim 29, wherein the number of contacts is N , and the
matrix is an $N \times N$ matrix.
34. A computer-readable medium storing computer-executable instructions
25 for causing a computer system to perform the method of claim 29.
35. A method of substrate modeling, comprising:
determining scalable parameters associated with at least three substrate contacts;

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constructing a matrix of the scalable parameters representative of the at least three substrate contacts; and

calculating resistance values associated with the at least three substrate contacts from the matrix.

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36. The method of claim 35, wherein the scalable parameters are Z parameters.

37. A computer-readable medium storing computer-executable instructions
10 for causing a computer system to perform the method of claim 35.

38. A method for determining a scalable Z parameter for a contact in a substrate, wherein the scalable Z parameter is associated with a resistance between the contact and a groundplane, the method comprising:

15 modeling the Z parameter as a function of contact area and contact perimeter, the function comprising at least one coefficient that is dependent on properties of the substrate;

obtaining a plurality of sample data points for the Z parameter in the substrate, the sample data points being obtained for a range of contact sizes; and

20 determining values of the multiple coefficients such that the function produces a curve that fits the sample data points.

39. The method of claim 38, wherein the range of contact sizes is from about $2.4\ \mu\text{m}$ to about $100\ \mu\text{m}$.

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40. The method of claim 38, wherein the contacts are square or rectangular.

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41. The method of claim 38, wherein at least a portion of the sample data points are obtained from a simulation or a measurement.

42. The method of claim 38, wherein the function is

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$$Z = \frac{1}{K_1 Area + K_2 Perimeter + K_3},$$

wherein Z is a ratio of an open-circuit voltage to input current for the contact with all other contacts in the substrate being open circuits, $Area$ is the contact area, $Perimeter$ is the contact perimeter, and K_1 , K_2 , and K_3 are coefficients that are dependent on the properties of the substrate.

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43. A computer-readable medium storing computer-executable instructions for causing a computer system to perform the method of claim 38.

44. A method for determining a scalable Z parameter for a pair of contacts in
15 a substrate, wherein the scalable Z parameter is associated with a cross-coupling resistance between a first contact and a second contact of the pair of contacts, the method comprising:

modeling the Z parameter as a function of a separation x between the first contact and the second contact, the function comprising multiple coefficients, at least
20 one of the multiple coefficients being dependent on properties of the substrate;

obtaining a plurality of sample data points for the Z parameter, the sample data points being obtained for a range of separations x between the first contact and the second contact; and

determining values of the multiple coefficients such that the function produces a
25 curve that fits the sample data points.

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45. The method of claim 44, wherein the first contact and the second contact have a same contact size.

46. The method of claim 44, wherein the range of separations x comprises
5 values of x substantially equal to or greater than $10\ \mu\text{m}$.

47. The method of claim 44, wherein the range of separations x is from about $10\ \mu\text{m}$ to about $120\ \mu\text{m}$.

10 48. The method of claim 44, wherein at least a portion of the sample data points are obtained from a simulation or a measurement.

49. The method of claim 44, wherein the function is

$$Z = \alpha e^{-\beta x},$$

15 wherein Z is a ratio of an open-circuit voltage at the first contact to a source current at the second contact, α is a value of Z for x_0 , and β is a coefficient that is dependent on the properties of the substrate.

50. The method of claim 49, wherein α is determined from

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$$\alpha = \frac{1}{K_1 Area + K_2 Perimeter + K_3},$$

wherein *Area* is a combined contact area, *Perimeter* is a perimeter of the combined contact, and K_1 , K_2 , and K_3 are coefficients that are dependent on the properties of the substrate.

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51. The method of claim 50, wherein K_1 , K_2 , and K_3 are determined by curve fitting α to a plurality of data points obtained for a range of different *Area* and *Perimeter* values.

5 52. A computer-readable medium storing computer-executable instructions for causing a computer system to perform the method of claim 44.

53. A method for determining a scalable Z parameter for a pair of contacts in a substrate, wherein the scalable Z parameter is associated with a cross-coupling
10 resistance between a first contact and a second contact of the pair of contacts, comprising:

modeling the Z parameter as a function of a relative position y between the first contact and the second contact, the first contact having a greater dimension than the second contact along a y axis, the function comprising multiple coefficients, at least one
15 of the multiple coefficients being scalable with dimensions of the first contact;

obtaining a plurality of sample data points for the Z parameter, the sample data points being calculated for a range of positions y of the second contact relative to the first contact; and

determining values of the multiple coefficients such that the function produces a
20 curve that fits the sample data points.

54. The method of claim 53, wherein the range of positions y is from substantially zero to a length of the first contact along its y axis.

25 55. The method of claim 54, wherein the plurality of data points are obtained for a contact having an area between about $2.4\ \mu\text{m}$ and $100\ \mu\text{m}$.

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56. The method of claim 53, wherein at least a portion of the sample data points are obtained from a simulation or a measurement.

57. The method of claim 53, wherein the function is

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$$Z = ay^2 + by + c,$$

wherein Z is a ratio of an open-circuit voltage at the first contact to a source current at the second contact, y is a relative position between the first contact and the second contact, and a , b , and c are scalable coefficients for the substrate that depend on contact dimensions.

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58. The method of claim 57, wherein c is found by:

$$c = \alpha e^{-\beta x_a}$$

wherein α is a value of Z for x_0 , β is a coefficient that is dependent on substrate properties, and x_a is a separation between the first contact and the second contact.

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59. The method of claim 57, wherein the pair of contacts is an original pair of contacts, and a , b , and c are scaleable for a new pair of contacts by a ratio of $\alpha_{\text{new}}/\alpha$, where α_{new} is a value of α for the new pair of contacts and α is a value of α for the original pair of contacts.

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60. A computer-readable medium storing computer-executable instructions for causing a computer system to perform the method of claim 53.

61. A method for determining a scalable Z parameter for a pair of contacts in
25 a substrate, wherein the Z parameter is associated with a cross-coupling resistance between a first contact and a second contact of the pair of contacts, comprising:

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modeling the scalable Z parameter as a function of a separation x between the first contact and the second contact and as a function of a relative position y between the first contact and the second contact, the first contact having a greater dimension than the second contact along a y axis, the function comprising multiple coefficients, at least one
5 of the multiple coefficients being scalable with dimensions of the first contact, and at least one of the multiple coefficients being dependent on substrate properties;

obtaining a first set of sample data points for the Z parameter, the first set of sample data points being obtained for a range of relative positions y of the second contact relative to the first contact for a fixed separation x ;

10 obtaining a second set of sample data points for the Z parameter, the second set of sample data points being obtained for a range of separations x for a fixed relative position y of the second contact; and

determining values of the multiple coefficients such that the function produces a curve that fits the sample data points.

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62. The method of claim 61, wherein the function is

$$Z = [ay^2 + by + c]e^{-\beta(x-x_a)},$$

wherein Z is a ratio of the open-circuit voltage at the first contact to the source current at the second contact, y is a relative position between the first contact and the second
20 contact, a , b , and c are scalable parameters for the substrate that depend on contact dimensions, x is a separation between the first contact and the second contact, x_a is a value of x used in determining a , b , and c , and β is a coefficient that is dependent on the properties of the substrate.

25 63. A computer-readable medium storing computer-executable instructions for causing a computer system to perform the method of claim 61.